Intelligent Systems: Reasoning and Recognition

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Support Vector Machines with Radial Basis Functions

A radial basis function (RBF) is a real-valued function whose value depends only on the distance from the origin. The Gaussian function

$$K(\|\vec{X} - \vec{X}_m\|) = e^{-\frac{\|\vec{X} - \vec{X}_m\|^2}{2}}$$

is a popular Radial Basis Function, and is often used as a kernel for support vector machines. When used in this way, each center point, \vec{X}_m , is one of the support vectors.

We can use a sum of N radial basis functions to define a discriminant function, where the support vectors are drawn from the M training samples. This gives a discriminant function

$$g(\vec{X}) = \sum_{m=1}^{M} a_m y_m K(||\vec{X} - \vec{X}_m||) + w_0,$$

The training samples \vec{X}_m for which $a_m \neq 0$ are the support vectors.

Suppose that you have two classes and a training data composed of 10 samples, $\{\vec{X}_m\}\{y_m\}$ and that an SVM learning algorithm has provided the weights $\{a_m\}$ as shown below, with b=0.

- a) Write out the equation for the discriminant function $g(\vec{X})$
- b) Is the training data separable with this discriminant function?

m	У	X_1	X_2	a_{m}
1	1	1	1	a _m 0 0
2	1	1	3	0
3	1	2	3 2	1
4	1	3	1	0
5	1	3 3	3	1 0 0
6	-1	1	3 5 5	0
7	-1	3	5	1
1 2 3 4 5 6 7 8	-1	3 5 5	1	0
9	-1	5	3 5	1
10	-1	5	5	0