

# Computer Vision

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Lesson 1

Exercises

## Homogeneous Coordinates and Projective Camera Models

1) Two lines make a point.  $\vec{P} = \vec{L} \times \vec{M}$

a) Use the cross product to derive the formula for the coefficients for the point  $\vec{P}$  at the intersection of two lines  $\vec{L}$ ,  $\vec{M}$

b) Derive the formula for the same coefficients using the determinant.

2) Two points make a line  $L^T = \vec{P} \times \vec{Q}$

a) Use the cross product to derive the formula for the coefficients for the line  $L^T$  passing through two points  $\vec{P}$ ,  $\vec{Q}$

b) Derive the formula for the same coefficients using the determinant.

3. Assume a camera at position  $(0, 0, 2)$  and orientation  $(-\pi/2, 0, 0)$  with focal length  $F$ , equipped with a  $512 \times 512$  pixel retina in which pixels are size  $0.02$  (mm/col) et  $0.01$  (mm/row) and an optical axis that intersects the retina at pixel  $(256, 256)$ .

a) Write the formula for the camera projective matrix  $\mathbf{M}_s^i$ .

b) A synchronization error causes each row to be shifted to the right by  $\alpha$  pixels.

Write the resulting transformation from retina to image  $\mathbf{C}_r^i$  as well as the resulting projective matrix  $\mathbf{M}_s^i$ .